

Name \_\_\_\_\_

Linear Motion	Rotational Motion	Relation between them:
$x$ (position, $m$ ):	$\theta$ (angle, $rad$ )	$x = r\theta$
$v$ (velocity, $m/s$ ): $v = \frac{\Delta x}{\Delta t}$ ,	$\omega$ (angular velocity, $rad/s$ ): $\omega = \frac{\Delta \theta}{\Delta t}$	$v = r\omega$
$a$ (acceleration, $m/s^2$ ): $a = \frac{\Delta v}{\Delta t}$	$\alpha$ (angular acceleration, $rad/s^2$ ): $\alpha = \frac{\Delta \omega}{\Delta t}$	$a = r\alpha$
Linear Kinematics	Rotational Kinematics	
$x = x_0 + v_0t + \frac{1}{2}at^2$	$\theta = \theta_0 + \omega_0t + \frac{1}{2}\alpha t^2$	
$v = v_0 + at$	$\omega = \omega_0 + \alpha t$	
$v^2 = v_0^2 + 2a(x - x_0)$	$\omega^2 = \omega_0^2 + 2\alpha(\theta - \theta_0)$	

Signs:  $\omega = +$  for counterclockwise,  $\omega = -$  for clockwise $\alpha = +$  for counterclockwise and speeding up,  $\alpha = -$  for counterclockwise and slowing down, $\alpha = -$  for clockwise and speeding up,  $\alpha = +$  for clockwise and slowing down

1. A wheel accelerates from rest. After 8 seconds the wheel made 3 revolutions.

- (a) What is the angular acceleration of the wheel in  $rad/s^2$ ?

- (b) What is the angular velocity in  $rad/s$  of the wheel after 8s?

2. A record on a record player starts from rest and begins rotating. The motor can accelerate the record at a rate of  $1rad/s^2$  and the manual says the record must be spinning at  $33rev/min$  before the music will play. How long will you have to wait until you hear the music?

How many revolutions will the record have made at that time?

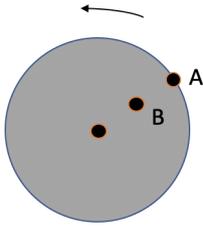
3. A car tire accelerates from rest to  $30m/s$  in a time of 6s. The radius of each tire is 0.2m. (Assume the tires rotate counterclockwise, so that the angular speed is positive.)

- (a) What is the acceleration of the car?

- (b) What is the angular acceleration of each tire?

- (c) Now the driver slams on the brake and the car decelerates down to  $20m/s$  in a time of 1s. What is the angular acceleration of each tire? (Is it positive or negative?)

4. Two points are on a disk rotating with a constant angular acceleration. The disk is speeding up. Point A is on the rim and Point B is halfway to the center of the disk. **A:**, **B:**, **C:** Same



- Which point moves through a greater distance after a certain amount of time:  $x$ ?
  - Which point turns through a greater angle,  $\theta$ ?
  - Which point has the greater linear (tangential) speed,  $v$ ?
  - Which point has the greater angular speed,  $\omega$ ?
  - Which point has the greater linear (tangential) acceleration,  $a$ ?
  - Which point has the greater angular acceleration,  $\alpha$ ?
  - Which point has the greater centripetal acceleration,  $a_c = \omega^2 r$ ?
5. Now consider the case of a penny-farthing bike. **A:**, **B:**, **C:** Same



- Which wheel moves through a greater distance after a certain amount of time:  $x$ ?
- Which wheel turns through a greater angle,  $\theta$ ?
- Which wheel has the greater linear (tangential) speed,  $v$ ?
- Which wheel has the greater angular speed,  $\omega$ ?
- Which wheel has the greater linear (tangential) acceleration,  $a$ ?
- Which wheel has the greater angular acceleration,  $\alpha$ ?
- Which wheel has the greater centripetal acceleration,  $a_c = \frac{v^2}{r}$ ?